

# Gluon saturation in $pA$ collisions at the LHC: predictions for hadron multiplicities

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The upcoming  $p + Pb$  run at the LHC will probe the nuclear gluon distribution at very small Bjorken  $x$  (from  $x \sim 10^{-4}$  at mid-rapidity down to  $x \sim 10^{-6}$  in the proton fragmentation region) and will allow to test approaches based on parton saturation. Here, we present the predictions of the KLN model for hadron multiplicities and multiplicity distributions in  $p + Pb$  collisions at a center-of-mass energy of 4.4 TeV. We also compare the model to the existing  $pp$ ,  $dA$  and  $AA$  data from RHIC and LHC.

Very soon, the Large Hadron Collider will record the first data on  $p + Pb$  collisions at the center-of-mass energy of 4.4 TeV. This data will allow to probe the nuclear gluon distributions at very small Bjorken  $x$ : from  $x \sim 10^{-4}$  at mid-rapidity down to  $x \sim 10^{-6}$  in the proton fragmentation region. Since the QCD evolution makes parton distributions increase at small  $x$ , the LHC experiments will allow to probe the nuclear wave functions at unprecedented parton densities. These measurements are crucial for testing the current theoretical approaches to high energy QCD.

Due to the breaking of scale invariance by quantum effects, QCD possesses a dimensionful scale  $\Lambda_{\text{QCD}}$  that determines the characteristic distance  $\sim \Lambda_{\text{QCD}}^{-1}$  at which the dynamics becomes non-perturbative. The asymptotic freedom [1, 2] makes the perturbative expansion valid only if a hard external scale  $Q^2 \gg \Lambda_{\text{QCD}}^2$  is present. Multiparticle production in hadron collisions is dominated by soft interactions and so in general is not amenable to the weak coupling treatment. However when the density of partons in the transverse plane  $Q_s^2$  becomes large compared to  $\Lambda_{\text{QCD}}^2$ , it regularizes the infrared behavior of the parton transverse momentum distributions at the “saturation momentum” [3]  $Q_s$  and thus prevents the running coupling of QCD from growing large,  $\alpha_s(Q_s) = g^2/4\pi \ll 1$  [3–5]. The gluon field  $A$  in this weak coupling regime has a large occupation number,  $A \sim 1/g > 1$  and can be treated as a classical “Color Glass Condensate” (CGC) [5–7].

While the complete theory of multi-particle production based on the ideas outlined above is still being developed, its main ingredients are clear and can serve as the basis for phenomenology. This was the motivation for the KLN model [8–10] combining the Glauber approach to proton-nucleus and nucleus-nucleus collisions (for a complete set of formulae see e.g. [11]) with a simple ansatz for the unintegrated parton distributions that accounts for the existence of a new dimensionful scale – the saturation momentum. The KLN model was successful in describing the RHIC data [12–15] on the centrality and rapidity dependence of charged hadron production in heavy ion collisions. The predictions for Pb Pb and p Pb collisions at the LHC were made in [16]. The comparison to the first LHC data [17] on hadron production in Pb-Pb collisions revealed that while the KLN model describes the centrality dependence rather well, the overall normalization exceeds the observed one by about 10-15 %. This implies that the energy dependence of the saturation momentum assumed in [16] was slightly too steep<sup>1</sup>.

Regarding  $pA$  collisions, we also have to remember that the number of “participants” (the nucleons that underwent at least one inelastic interaction) in this case is much smaller than in  $A A$  collisions, and that fluctuations are much more important. Therefore a Monte-Carlo (MC) based formulation [18] of the numerical integration of the KLN model [19] can be expected to provide more accurate predictions. Indeed, the MC method leads to a better agreement between the data and the model prediction [20] in d Au collisions at RHIC. The MC based KLN model [18] has been used to generate initial conditions for the hydrodynamical description of collective flow, see e.g. [21–23].

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<sup>1</sup> While it is evident that the model has to be refined, let us put this discrepancy in perspective by noting that some of the early pre-RHIC predictions for the LHC that did not take into account the concepts of parton saturation and coherence overestimated the measured hadron multiplicity by almost an order of magnitude.

The goal of this letter is to provide updated predictions for p Pb collisions at the LHC. Let us explicitly list the differences between the present and the previous [16] papers: i) we consider the c.m.s. energy of the forthcoming p Pb run – 4.4 TeV; ii) we have reduced the intercept describing the energy dependence of saturation momentum by  $\sim 20\%$ ; iii) we employ the MC method of evaluating the number of participants. Of course, after making these changes we have to make sure that the RHIC data is still adequately described – therefore we present the comparison to the RHIC AA and dA as well. While these changes may seem insignificant, the p Pb LHC data present a chance to test saturation ideas, and this requires quantitative predictions made to the best of our current knowledge.

Let us briefly recall the basic ingredients of the KLN approach; for details, see [9, 16]. The multiplicity per unit rapidity

$$\frac{dN}{dy} = \frac{K}{S} \int dp_t^2 \left( E \frac{d\sigma}{d^3p} \right) = \frac{K}{S} \frac{4\pi N_c \alpha_S}{N_c^2 - 1} \int_0^\infty \frac{dp_t^2}{p_t^4} x_2 G_{A_2}(x_2, p_t^2) x_1 G_{A_1}(x_1, p_t^2), \quad (1)$$

is evaluated using the gluon density obtained from a simple ansatz for the unintegrated gluon distribution [9] encoding the saturation phenomenon:

$$xG(x, p_t^2) = \begin{cases} \frac{S}{\alpha_s(Q_s)} p_t^2 (1-x)^4, & p_t < Q_s(x) \\ \frac{S}{\alpha_s(Q_s)} Q_s^2 (1-x)^4, & p_t > Q_s(x) \end{cases} \quad (2)$$

where  $x = x_1$  or  $x_2$ , with  $x_{1,2} = (p_t/W)e^{\pm y}$ ; the  $+$ ( $-$ ) sign in the exponent applies to the projectile (target), and  $W \equiv \sqrt{s}$  is the c.m.s. energy. The factor  $S$  in eq. (1) is the transverse area involved in the collision (see below). The normalization factor  $K$  describes the conversion of partons to hadrons and is determined by a global fit to  $pp$  data at various energies, and to  $d + Au$  data from RHIC.

To describe the running of QCD coupling, we use the  $\beta$ -function in the one-loop approximation with  $N_f = 3$  light quark flavors and  $\Lambda_{\text{QCD}}^2 = 0.05 \text{ GeV}^2$  but assume that the coupling freezes at  $\alpha_{\text{max}} = 0.52$  [24]:

$$\alpha_s(Q^2) = \min \left[ \frac{12\pi}{27 \log \frac{Q^2}{\Lambda_{\text{QCD}}^2}}, \alpha_{\text{max}} \right], \quad (Q^2 \geq \Lambda_{\text{QCD}}^2). \quad (3)$$

The factor of  $\alpha_s(Q^2)$  in the integral (1) is evaluated at the scale  $p_t^2$ , if this is the largest scale, or else at the lower of  $Q_{s,P}^2(y)$  and  $Q_{s,T}^2(y)$ . The saturation momenta are defined as

$$Q_s^2(y) = Q_0^2 N_{\text{part}} \left( x_0 \frac{W}{Q_0} e^{\mp y} \right)^{\bar{\lambda}}, \quad (4)$$

where again the  $+$ ( $-$ ) sign in the exponent applies to the projectile (target). We fix the parameters to  $Q_0 = 0.6 \text{ GeV}$ ,  $x_0 = 0.01$ , and  $\bar{\lambda} = 0.205$ . In the midrapidity region of collisions at RHIC energy, this results in a gluon saturation momentum  $Q_s \simeq 0.68 \text{ GeV}$  for a proton. On account of the large radius of the deuteron, we have used  $N_{\text{part,P}} = 1$  in (4) in this case assuming that the parton substructure of the nucleon in the deuteron is not modified. For minimum bias  $d + Au$  collisions we multiply  $dN/dy$  by a factor of 1.52 which is our estimate for the corresponding equivalent number of  $p + Au$  collisions at an energy of  $W = 200 \text{ GeV}$ . For  $pp$  collisions we choose the effective area  $S_{pp} \simeq 0.7 S_{pA}$  somewhat smaller than for  $pA$  collisions, as suggested by the data. This may be an indication that in proton-proton collisions only part of the proton takes part in the interaction. On the other hand, the large nucleus makes all of the proton's constituents to interact.

To evaluate the pseudo-rapidity distributions, Eq. (1) needs to be rewritten using the transformation

$$y(\eta) = \frac{1}{2} \log \frac{\sqrt{\cosh^2 \eta + \mu^2} + \sinh \eta}{\sqrt{\cosh^2 \eta + \mu^2} - \sinh \eta} \quad (5)$$

with the Jacobian

$$J(\eta) = \frac{\partial y}{\partial \eta} = \frac{\cosh \eta}{\sqrt{\cosh^2 \eta + \mu^2}}. \quad (6)$$

The scale  $\mu^2(W)$  is allowed to exhibit a weak energy dependence according to

$$\mu(W) = \frac{0.24}{0.13 + 0.32 W^{0.115}}, \quad (7)$$

with  $W$  expressed in units of TeV. This parameterization reproduces approximately the “shoulder” structure of  $dN/d\eta$  observed in symmetric  $pp$  collisions. We did not modify  $\mu(W)$  for the case of  $pA$  collisions.

The multiplicity discussed above represents the *average* multiplicity  $\langle N_{\text{ch}} \rangle$  observed in collisions with a fixed number of participants. In experiment, the multiplicity fluctuates both due to the fluctuations in the number of participants and due to “intrinsic” fluctuation at fixed number of participants. To model the “intrinsic” fluctuations of the number of produced particles we consider the multiplicity (per unit rapidity) as a random variable distributed according to a negative binomial distribution,

$$P(N_{\text{ch}}) = \frac{\Gamma(k+n)}{\Gamma(k)\Gamma(n+1)} \frac{\langle N_{\text{ch}} \rangle^{N_{\text{ch}}} k^k}{(\langle N_{\text{ch}} \rangle + k)^{N_{\text{ch}}+k}} . \quad (8)$$

The quantity  $k$  which characterizes the fluctuations in the saturation approach has been estimated as be [25, 26]

$$k = \kappa \frac{N_c^2 - 1}{2\pi} Q_s^2(y, W) \sigma_k(W) . \quad (9)$$

In our numerical estimates we have assumed that  $\sigma_k(W) = \sigma_{\text{in}}(W)/10$  is proportional to the inelastic  $pp$  cross section, and that  $Q_s$  is the saturation scale of the proton. We find that the value of  $\kappa$  which describes best the multiplicity distributions in  $pp$  collisions is about  $\kappa \simeq 0.05$ .

All observables for  $pA$  collisions finally need to be averaged also over an ensemble of  $N_{\text{part,A}}$ , which enters through eq. (4). We obtain the number of participants in the heavy ion target from a Monte-Carlo Glauber simulation<sup>2</sup>: assume a uniformly distributed random number  $0 < \nu < 1$  and let

$$N_{\text{part,A}}(\vec{b}) = \sum_{i=1 \dots A} \Theta \left( P(\vec{b} - \vec{r}_i) - \nu_i \right) . \quad (10)$$

Here,  $b$  is the impact parameter of the  $p + A$  collision, i.e. the transverse distance of the proton from the center of the target nucleus; it is a random variable with the probability density  $b db$ . The set  $\{\vec{r}_i\}$  corresponds to the coordinates of the nucleons in the target which are picked randomly according to a Woods-Saxon distribution. Finally,  $P(r)$  denotes the interaction probability of two nucleons separated by a transverse distance  $r$ ; for simplicity, here we assume “hard sphere” nucleons:

$$P(r) = \Theta \left( \sqrt{\frac{\sigma_{\text{in}}(W)}{\pi}} - r \right) . \quad (11)$$

We use the measured values  $\sigma_{\text{in}}(s) = 42, 52, 60, 65.75, 70.45$  mb at  $W = 200, 900, 2360, 4400, 7000$  GeV, respectively.

Let us now present and describe our results. First we re-check the model against the RHIC data. Fig. 1 shows the comparison to the d Au data; in the range  $-1 < \eta < 2$  the agreement is satisfactory. Note that at  $\eta \gtrsim 2$  the saturation momentum of the projectile becomes small and so the validity of the saturation approach is questionable at best. Also, in the fragmentation region of the nucleus one would have to account for the contribution from valence quarks to improve agreement with the data.

The centrality dependence of the charged particle multiplicity in Au+Au collisions at RHIC is shown at Fig. 2; the agreement is very good. The reduction of the intercept of the gluon distribution (by  $\sim 20\%$  in comparison to [16]) allows us to reproduce well also the LHC Pb+Pb data, see Fig. 2. Figs. 3,4,5 show the comparison of our model to the pp data from the LHC on charged hadron multiplicities and multiplicity distributions at  $\sqrt{s} = 0.9, 2.36$  and 7 TeV, respectively. The agreement is seen to be quite good. Finally, in Figs. 6,7 we present our predictions for the upcoming p Pb run at  $\sqrt{s} = 4.4$  TeV.

To summarize, we have presented updated predictions of the KLN model for p Pb collisions at the LHC, as well as comparisons to the RHIC and LHC data on hadron multiplicities and multiplicity distributions. Clearly, our treatment has been somewhat model-dependent and involves a few adjustable parameters. Nevertheless, our model does capture the emergence of a new dimensionful scale governing QCD interactions at high energies, and thus

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<sup>2</sup> On the other hand, in AA collisions the fluctuations of  $N_{\text{part}}$  do not affect the multiplicity strongly; we have calculated  $N_{\text{part}}$  directly, in a “mean field approximation”, from a nuclear Woods-Saxon distribution.

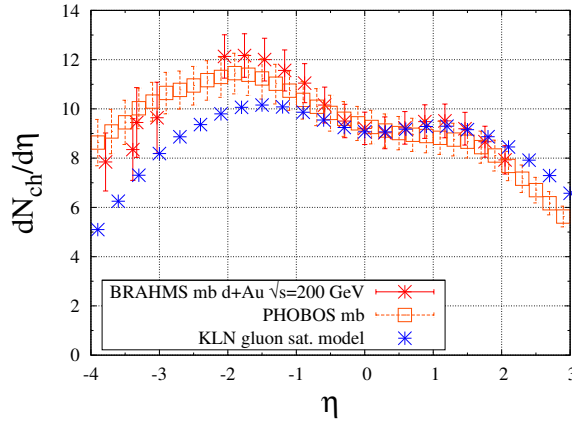


FIG. 1: Rapidity distribution of charged particles in minimum bias  $d+Au$  collisions at  $W = 200$  GeV. PHOBOS and BRAHMS data from refs. [30, 31].

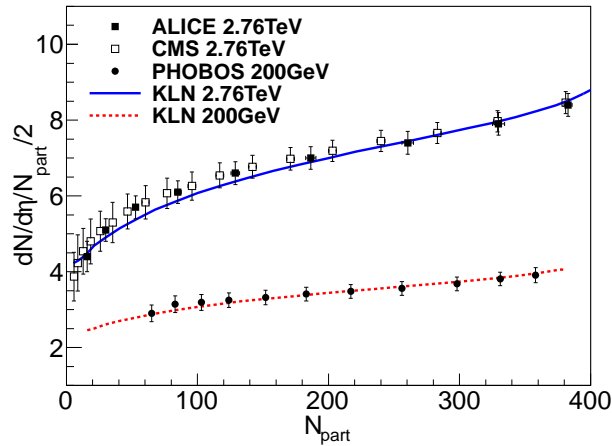


FIG. 2: Centrality dependence of the charged hadron multiplicity at  $\eta = 0$  in  $AuAu$  collisions at  $W = 200$  GeV [14] and  $PbPb$  collisions at  $W = 2.76$  TeV [17, 27]

expresses in quantitative form the essence of the parton saturation phenomenon. The comparison of our model to the existing Pb Pb and the forthcoming p Pb data would also allow to deduce the amount of additional entropy produced during the evolution of the quark-gluon fluid in heavy ion collisions [32]. Our present treatment assumes no additional entropy production, which corresponds to the zero viscosity limit; a deviation from our prediction could signal the presence of viscous effects.

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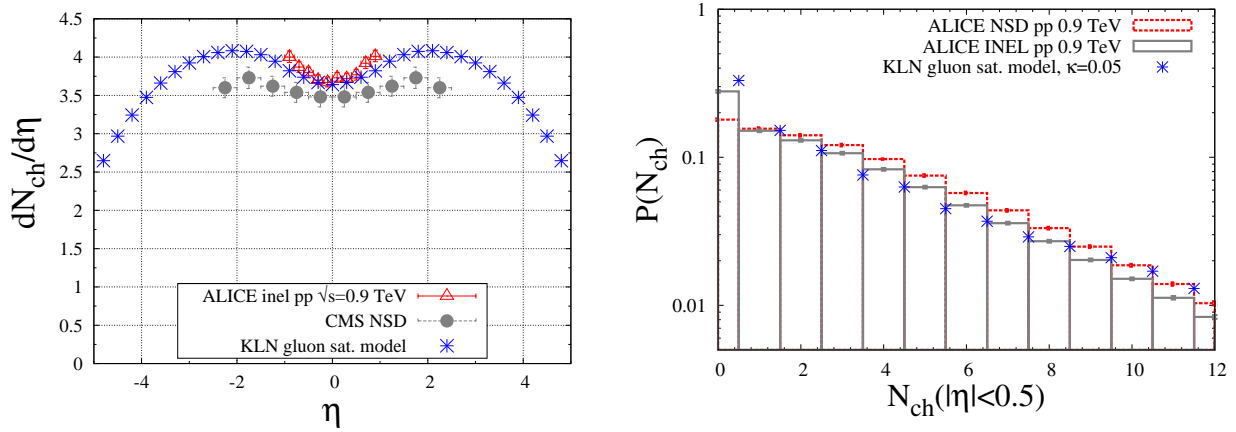


FIG. 3: Left: rapidity distribution of charged particles in  $pp$  collisions at  $W = 900$  GeV. Right: Charged particle multiplicity distribution. ALICE and CMS data from refs. [28, 29].

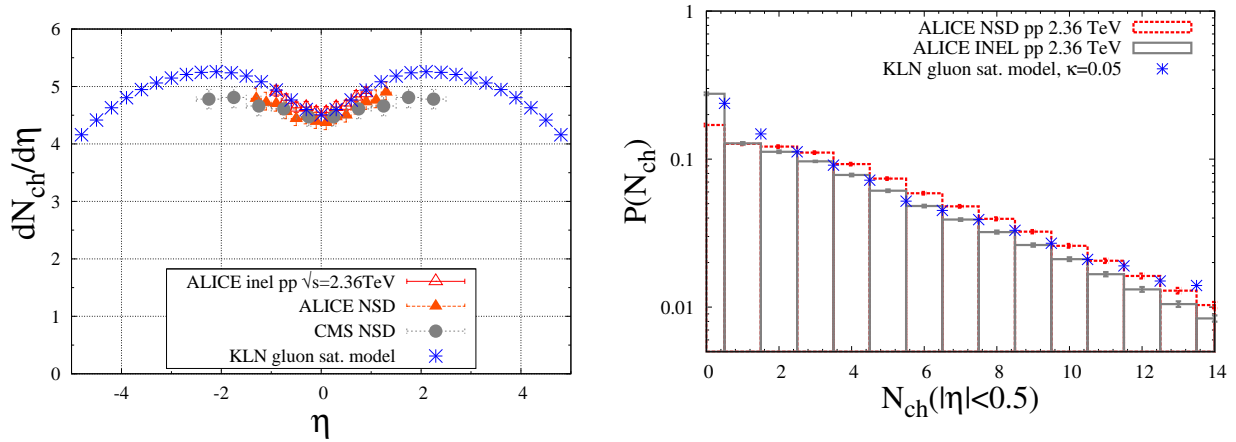


FIG. 4: Left: rapidity distribution of charged particles in  $pp$  collisions at  $W = 2360$  GeV. Right: Charged particle multiplicity distribution. ALICE and CMS data from refs. [28, 29].

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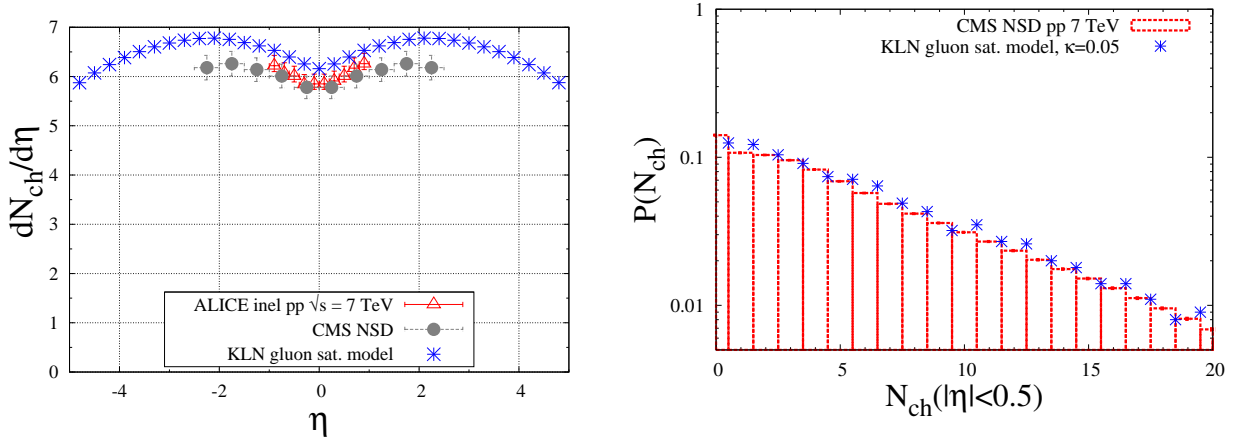


FIG. 5: Left: rapidity distribution of charged particles in  $pp$  collisions at  $W = 7000$  GeV. Right: Charged particle multiplicity distribution. ALICE and CMS data from refs. [28, 29].

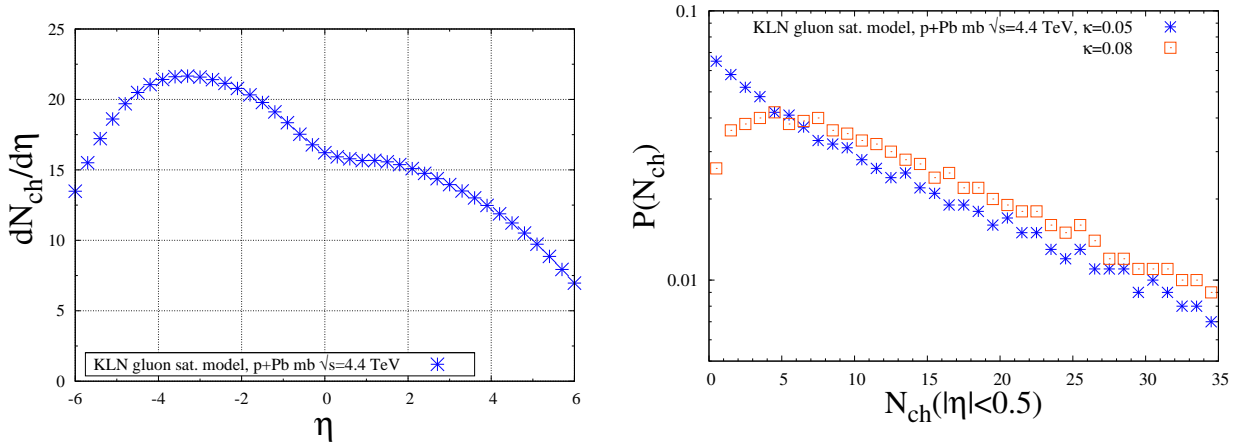


FIG. 6: Left: rapidity distribution of charged particles in minimum bias  $p + Pb$  collisions at  $W = 4400$  GeV. A  $\sim 10\%$  overall normalization uncertainty is not shown explicitly. Right: Charged particle multiplicity distribution.

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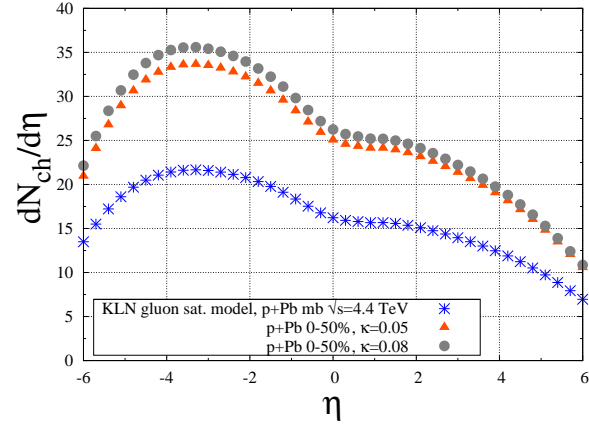


FIG. 7: Rapidity distribution of charged particles in  $p + Pb$  collisions at  $W = 4400$  GeV for minimum bias trigger and for the 0-50% centrality/multiplicity class. A  $\sim 10\%$  overall normalization uncertainty is not shown explicitly.

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**Note added Oct. 19, 2012:**

After our paper was published, data from the ALICE Collaboration on the charged hadron multiplicity in p+Pb collisions at  $\sqrt{s} = 5.02$  TeV appeared [33]. The agreement between the data and our prediction is quite good over the entire pseudo-rapidity range of the data,  $-2 < \eta < +2$ . However, while at  $\eta = 0$  our prediction essentially coincides with the data, towards the nuclear fragmentation region, at  $\eta \simeq -2$ , the prediction deviates from the data by about 10%, see open boxes in Fig. 8. Here we would like to point out that this small discrepancy is within the uncertainty resulting from the Jacobian of the transformation from rapidity to pseudo-rapidity, see eqs. (5,6,7), and that it can be easily eliminated.

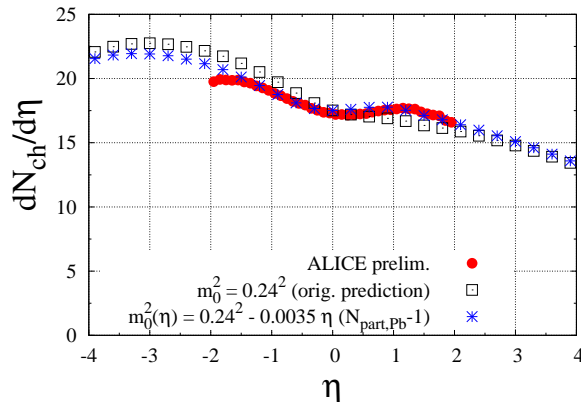


FIG. 8: Rapidity distribution of charged particles in minimum bias  $p + Pb$  collisions at  $W = 5000$  GeV. For these curves we have also accounted for the boost of the  $\eta = 0$  lab frame by adding a rapidity shift of  $\Delta y = \frac{1}{2} \log 82/208 \simeq -0.4654$  to the right-hand-side of eq. (5).  $m_0$  denotes the numerator from eq. (7).

In our paper, we assumed that the value of the parameter  $\mu$  (determined by the typical mass and transverse momentum of the produced hadrons) in  $pA$  collisions is the same as in  $pp$  collisions, and is given by eq. (7). A more accurate approximation is to assume that the typical transverse mass of the produced hadrons is determined by the transverse momentum distribution of the produced gluons. This leads to the assumption (see e.g. eq. (27) in [9]) that the parameter  $\mu^2$  decreases when the saturation momentum grows, i.e. that it varies with the pseudo-rapidity and the participant density in the Pb nucleus as:

$$\mu^2(\eta) = \frac{0.24^2 - a \eta [N_{\text{part(Pb)}} - 1]}{(0.13 + 0.32 W^{0.115})^2}, \quad (12)$$

where  $a$  is a parameter reflecting the rapidity dependencies of saturation momentum and of the typical mass of produced hadrons. The sign of the second term describes the growth of the saturation momentum of the nucleus at small  $x$ , towards the proton fragmentation region (positive  $\eta$ ). The (presumably small) magnitude of the parameter  $a$  is determined to large extent by non-perturbative fragmentation phenomena. In Fig. 8 we show the result of our computation with  $a = 0.0035$ . One can see that a small adjustment of the Jacobian of rapidity-to-pseudorapidity transformation that is motivated by the expected features of hadron production leads to near-perfect agreement with the data.